PARALLEL ITERATIVE METHODS FOR SOLVING THE COMMON NULL POINT PROBLEM IN BANACH SPACES

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ABSTRACT. We consider the common null point problem in Banach spaces. Then, using the hybrid projection method and the ε-enlargement of maximal monotone operators, we prove two strong convergence theorems for finding a solution of this problem.

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